

# **Nano-scale CMOS and Low Voltage Analog to Digital Converter Design Challenges**

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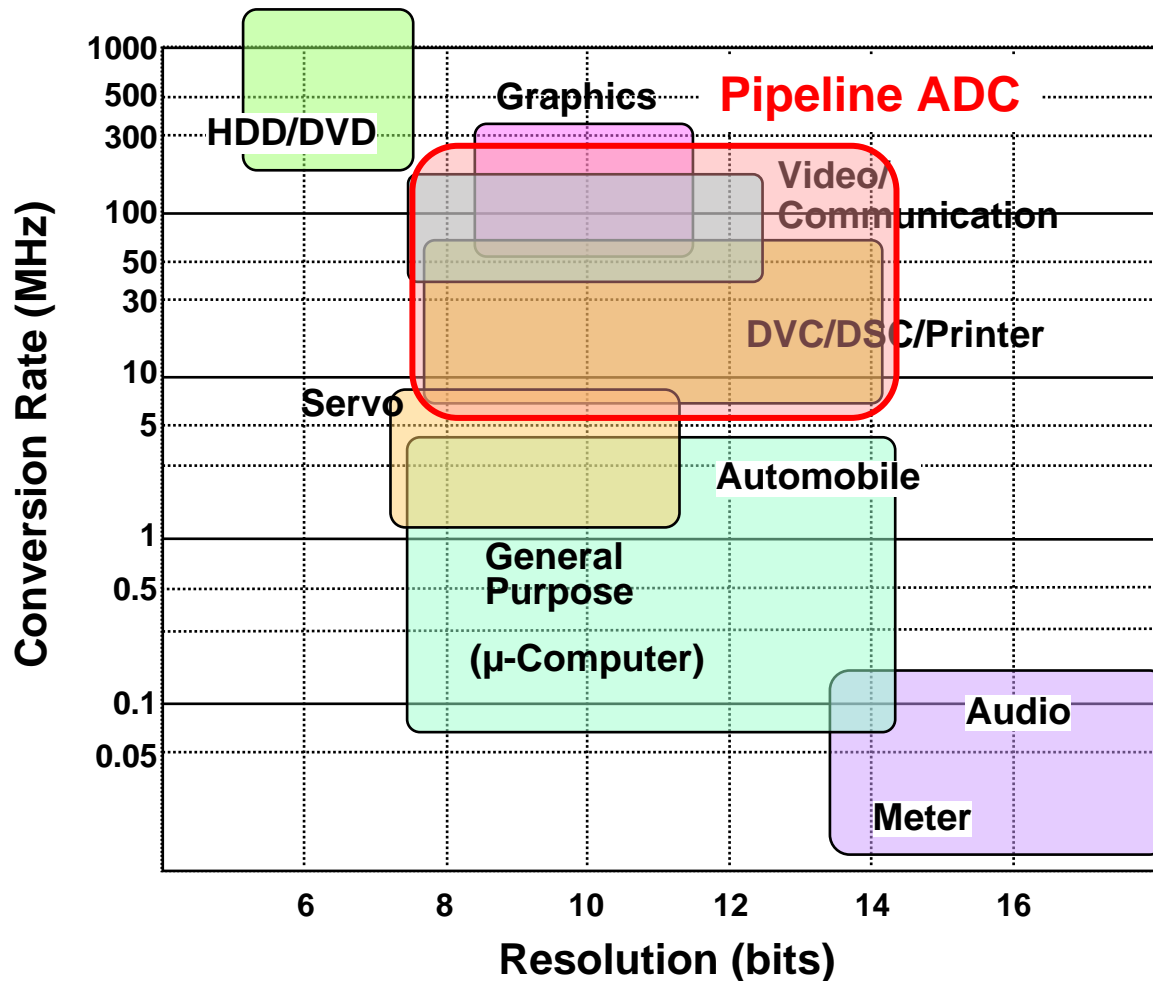
--- No use of Operational amplifier --

- Comparator controlled current source
- Successive approximation ADC
- Sub-ranging ADC

## 4. Summary

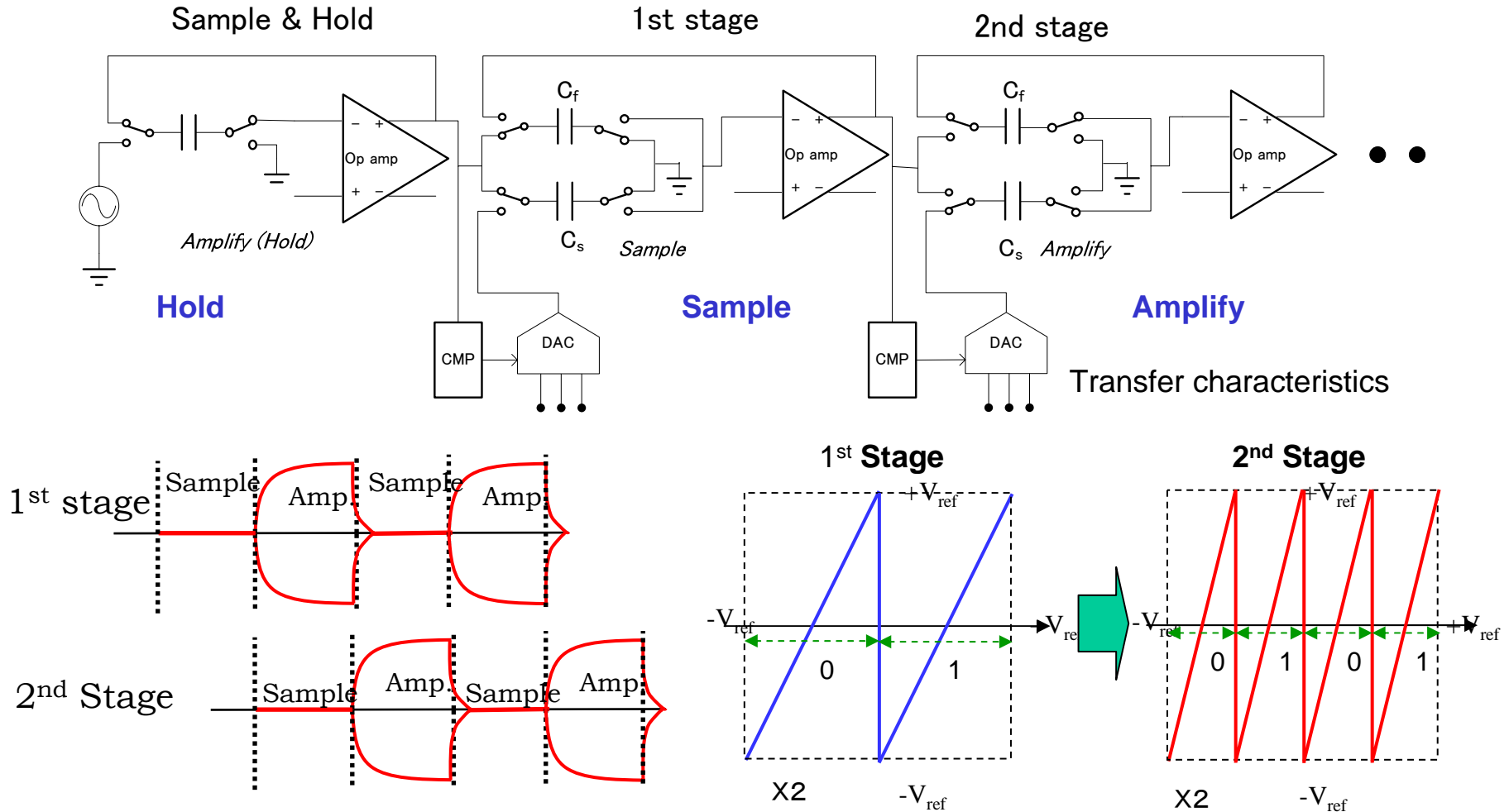
# Performance and applications

Pipeline ADC is the major conversion architecture for communications and digital consumer products.



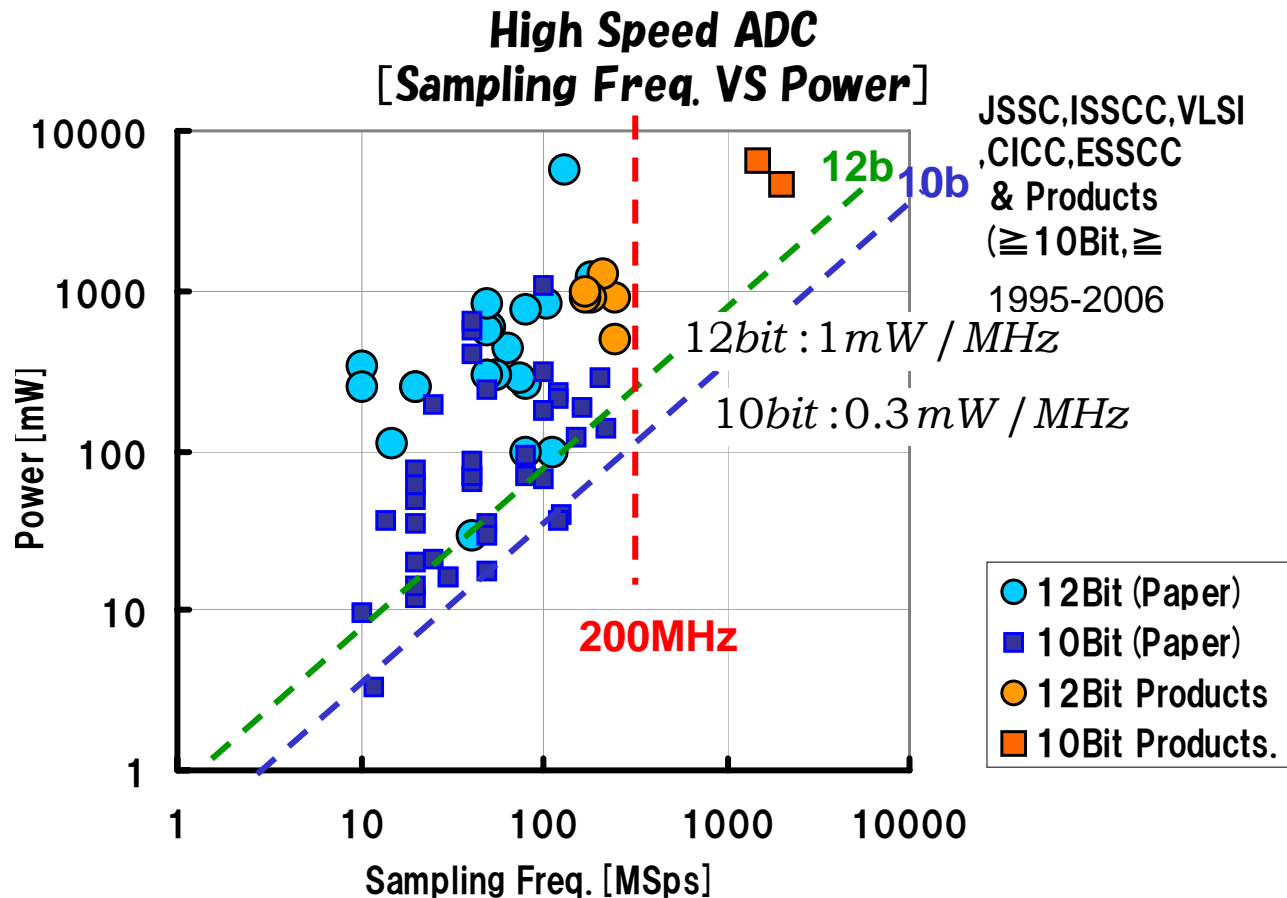
# Pipeline ADC

Folding I/O characteristics makes higher resolution along with pipeline stages.



# Speed and power

Conversion speed has saturated at 200 MHz  
Smaller mW/MHz is needed for low power operation.  
0.3mW/MHz for 10bit and 1mW/MHz for 12bit are the bottom lines.



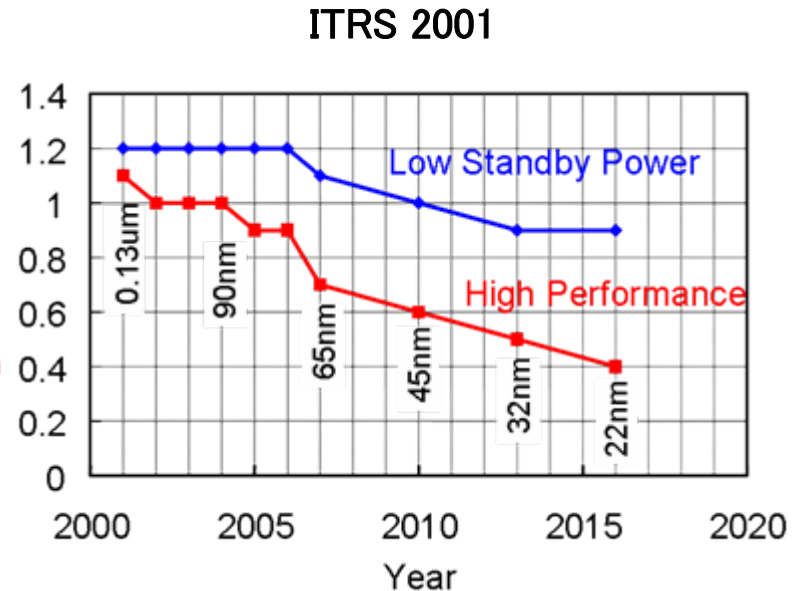
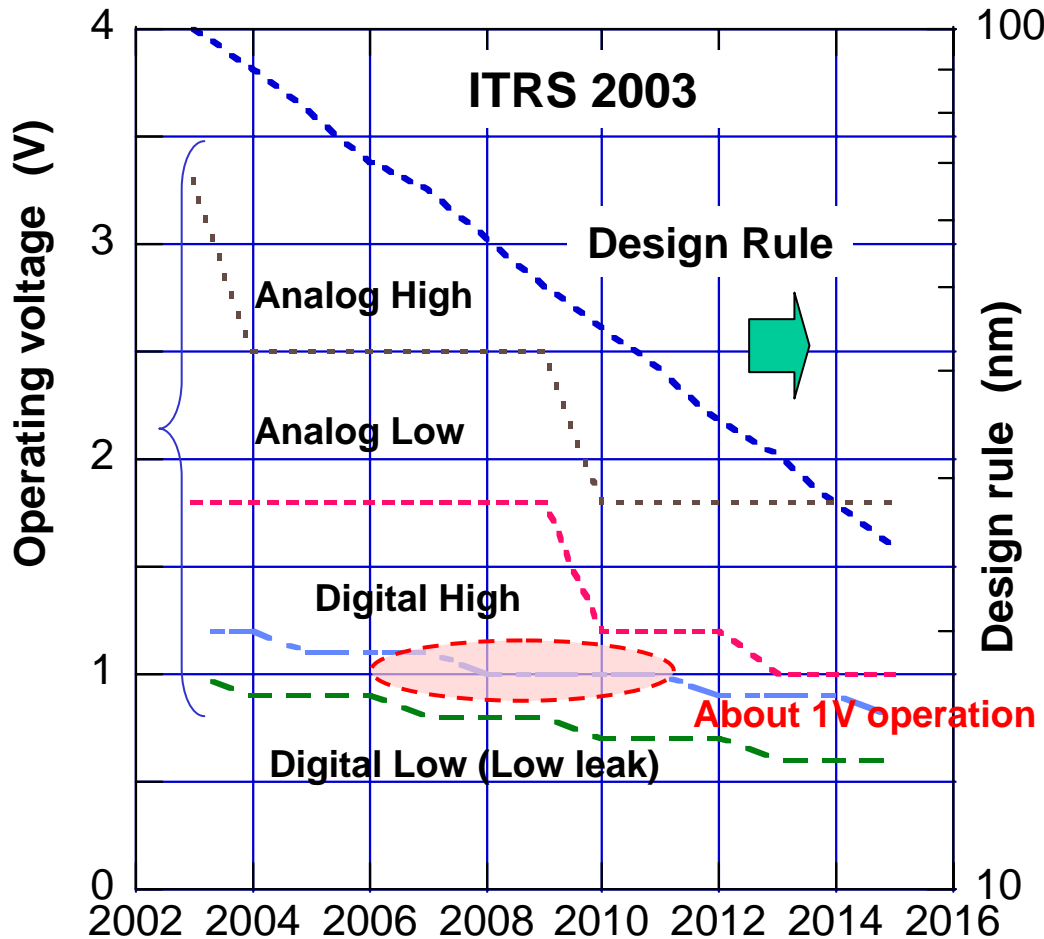
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# **Effect of technology scaling on analog performance**

## **Technology scaling and performance of pipeline ADC**

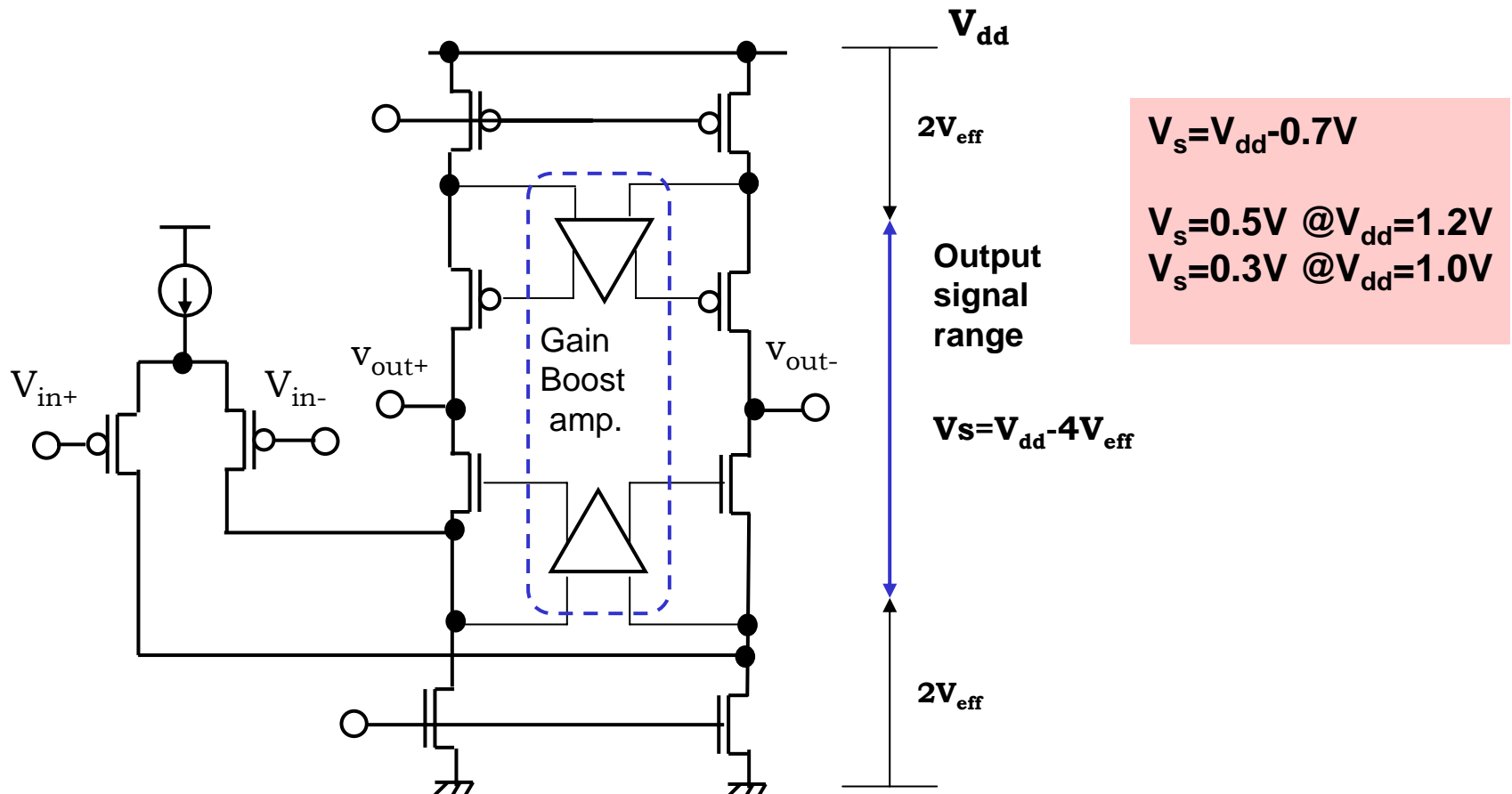
# Operating voltage trend

Operating voltage of scaled device will keep about 1V



# Operational amplifier for ADC

Pipeline ADC needs high performance amplifier.  
The output signal range will be reduced along with voltage lowering.



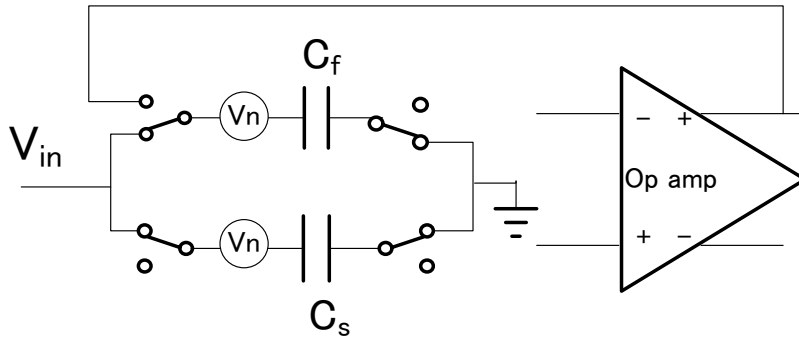


# Requirements for operational amplifier

Higher resolution requires higher open loop gain.

Higher conversion frequency requires higher closed loop GBW.

## Sampling



## DC gain

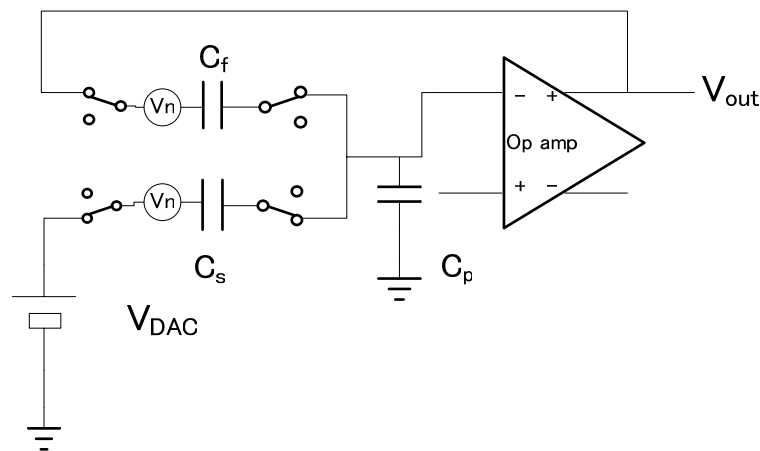
$$G_{error} \approx -\frac{1}{G} \left( 2 + \frac{C_p}{C_f} \right) \approx -\frac{1}{G\beta}$$

$$\frac{1}{G} \leq \frac{\beta}{2^{N-M+1}}$$

N: ADC resolution  
M: Stage resolution

$$\beta \equiv \frac{1}{\left( 2 + \frac{C_p}{C_f} \right)}$$

## Amplify



$$G (dB) > 6N + 10 \text{ for 1.5b pipeline ADC}$$

## Closed loop gain-bandwidth

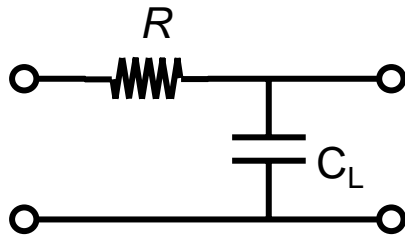
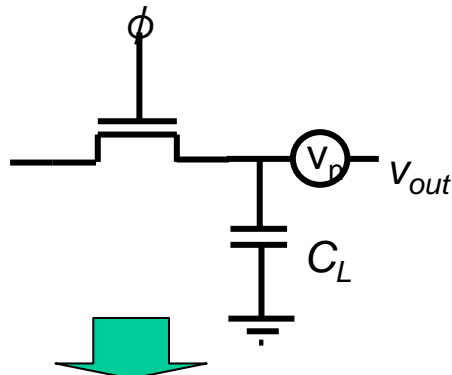
$$GBW_{close} = \frac{g_m \beta}{2\pi C_L} > \frac{N \cdot fc}{3}$$

$$\beta = \frac{C_f}{C_f + C_s + C_{pi}}$$

$$C_L = C_{po} + C_{oL} + \frac{C_f (C_s + C_{pi})}{C_f + C_s + C_{pi}}$$

# kT/C noise

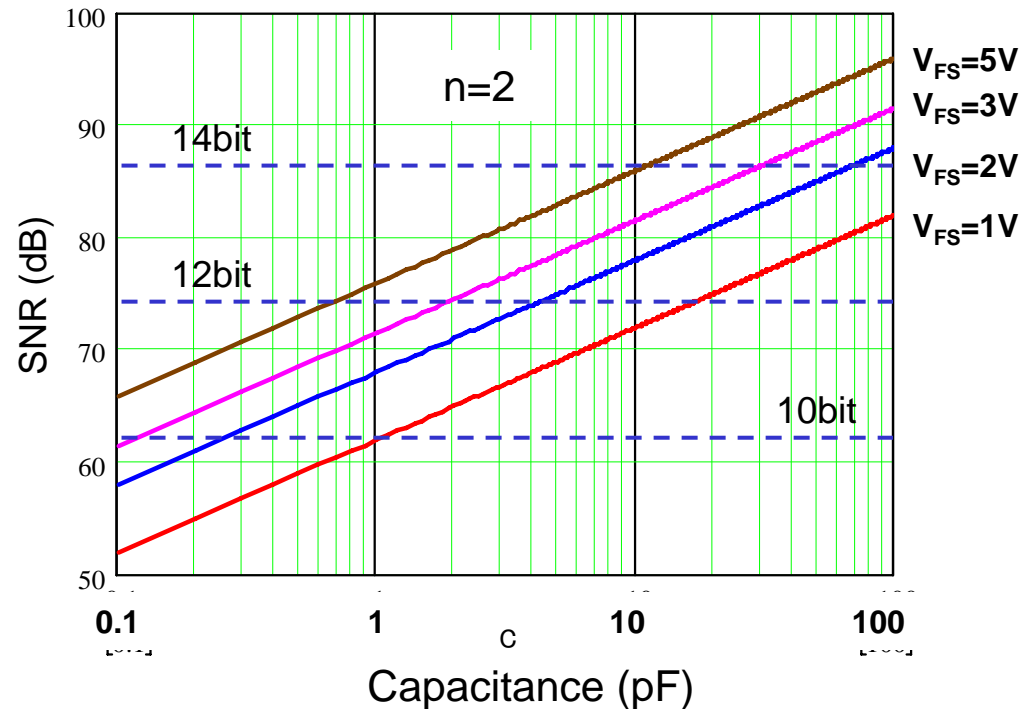
Larger SNR requires larger capacitance and larger signal swing.  
Low signal swing increases required capacitance.



$$\langle v_n^2 \rangle = 4kTR \int \frac{1}{1 + (\omega CR)^2} \frac{d\omega}{2\pi} = \frac{kT}{C}$$

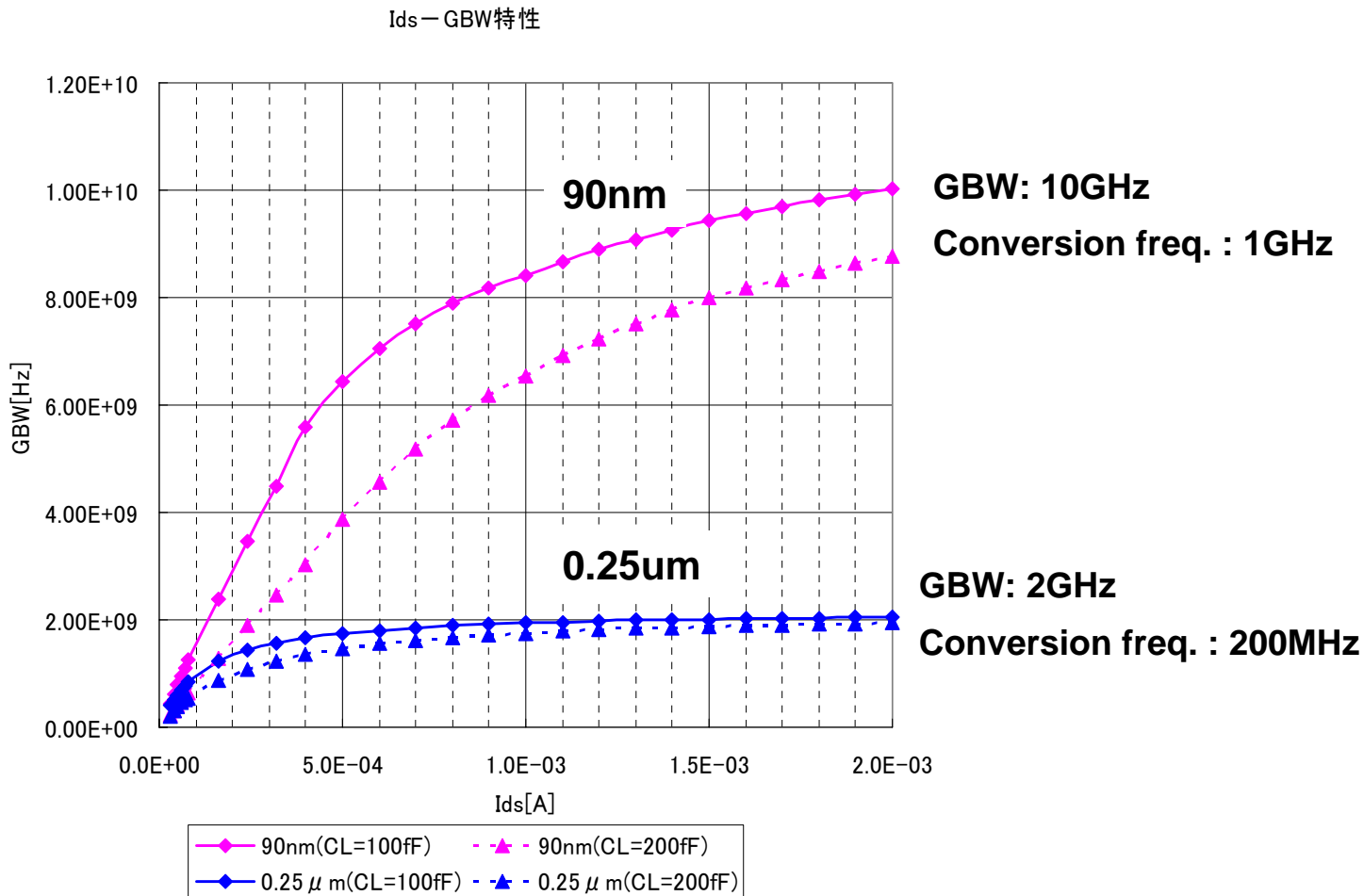
$$v_n^2 = \frac{nkT}{C} \quad n: \text{configuration coefficient}$$

$$SNR(dB) = 10 \log \left( \frac{CV_{FS}^2}{8nkT} \right)$$



# Effect of technology scaling

Gain bandwidth of OpAmp increases along with technology scaling.  
However, can we increase every needed performances for ADCs?

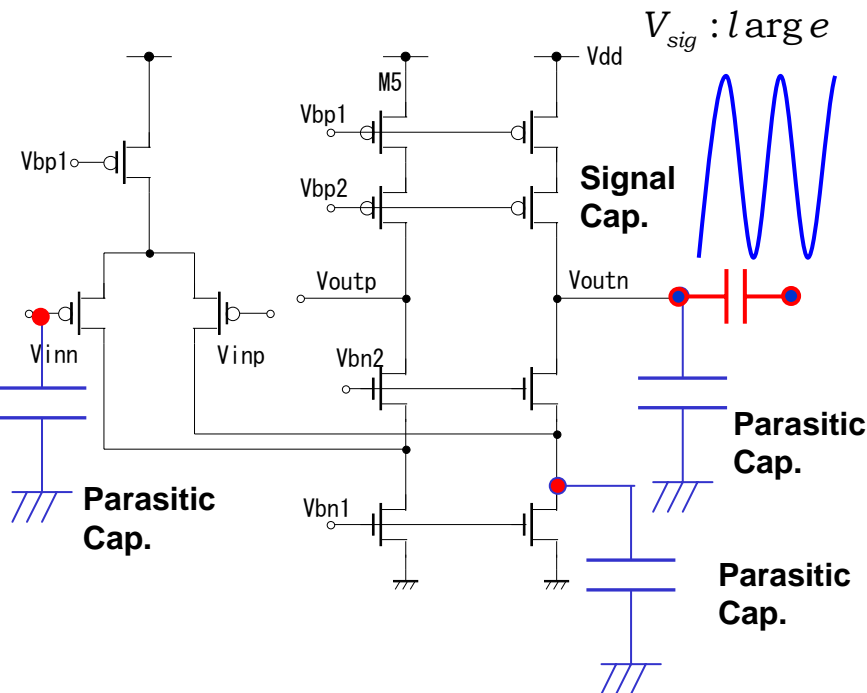


# Technology scaling for analog

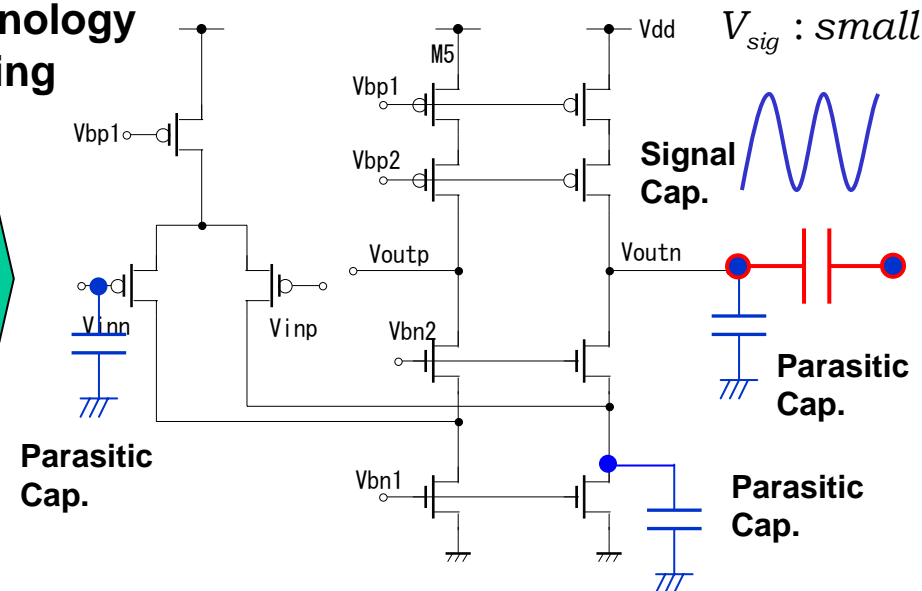
Technology scaling can reduce parasitic capacitances.  
However signal capacitance will increase to keep the same SNR at lower voltage operation.

Parasitic capacitance → smaller  
Operating voltage → lower  
Signal swing → lower

Signal capacitance → larger  
Voltage gain → lower

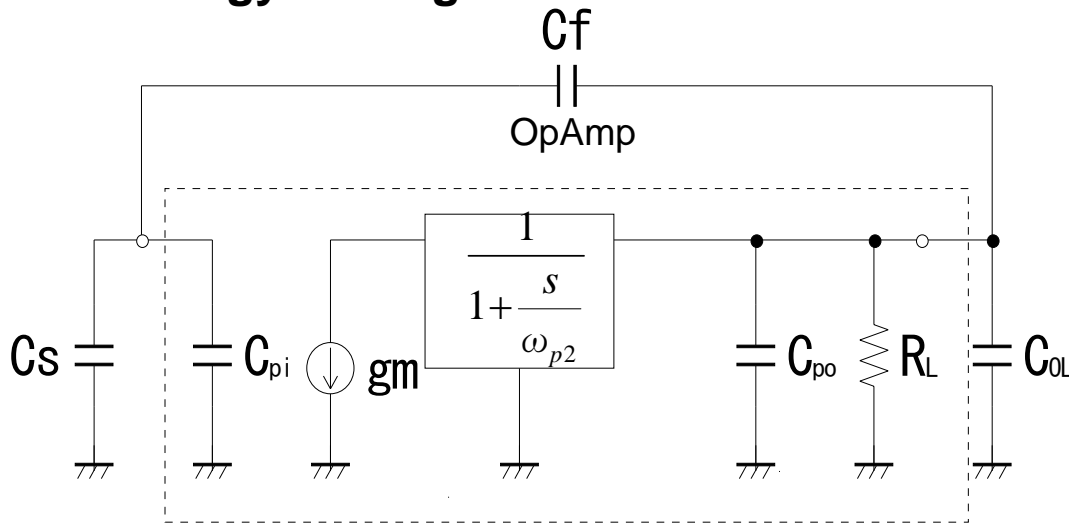


Technology scaling



# Performance model for pipeline ADC

We have developed the performance model for pipeline ADC that can treat technology scaling.



$g_m$  : Transconductance of input stage  
 $C_s, C_f$  : Signal capacitance for feedback loop  
 $C_{pi}, C_{po}$  : input & output parasitic capacitance  
 $C_{oL}$  : Load capacitance  
 $R_L$  : Output resistance  
 $\omega_{p2}$  : Second pole of OpAmp

A. Matsuzawa, "Analog IC Technologies for Future Wireless Systems," IEICE, Tan on Electronics, Vol. E89-C, No.4, pp. 446-454, April, 2006.

$$GBW_{-close} = \frac{g_m}{2\pi C_L} \beta$$

$$\beta = \frac{C_f}{C_f + C_s + C_{pi}}$$

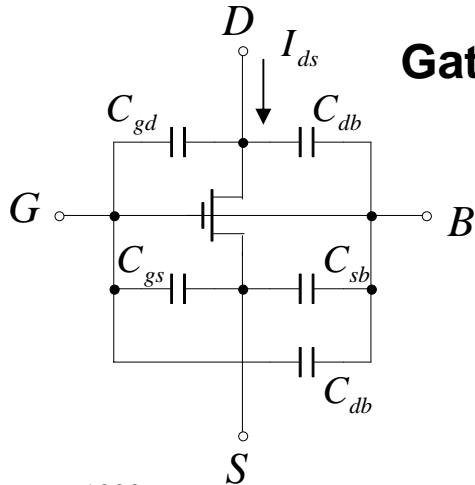
$$C_L = C_{po} + C_{oL} + \frac{C_f(C_s + C_{pi})}{C_f + C_s + C_{pi}}$$

$$C_{oL} = \frac{C_s + C_f}{2} \quad C_o = C_s = C_f = C_{oL}$$

$$GBW_{-close} = \frac{g_m}{2\pi C_o} \frac{1}{\left(2 + \frac{C_{pi}}{C_o}\right) \left(1 + \frac{C_{po}}{C_o}\right) + \left(1 + \frac{C_{pi}}{C_o}\right)} = \frac{I_{ds}}{\pi C_o V_{eff}} \frac{1}{\left(2 + \frac{\alpha_{pi} I_{ds}}{C_o}\right) \left(1 + \frac{\alpha_{po} I_{ds}}{C_o}\right) + \left(1 + \frac{\alpha_{pi} I_{ds}}{C_o}\right)}$$

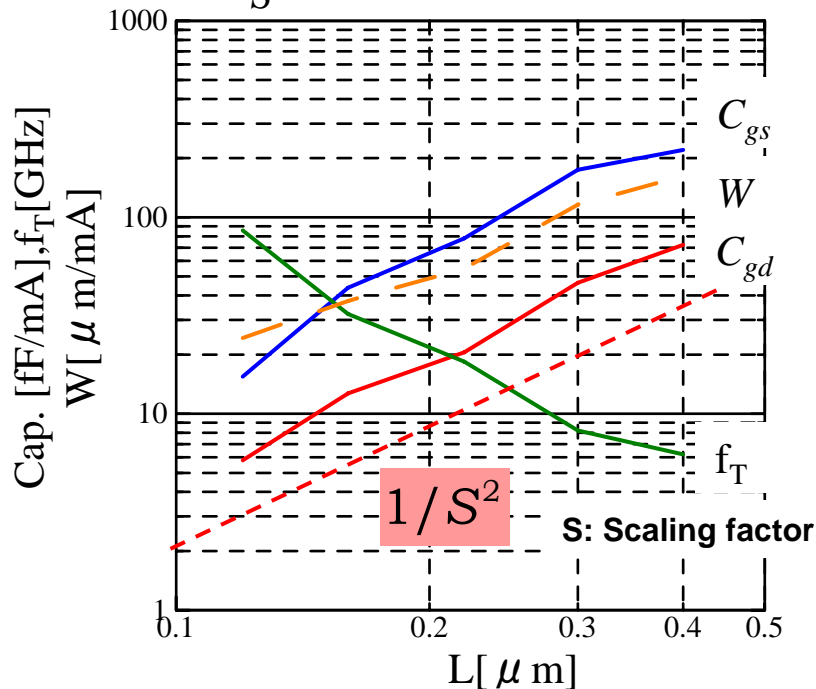
# Scaling and analog device and circuit parameters

Gate width and capacitances decrease with technology scaling.



$$V_{eff} = 0.175V$$

$$W = \frac{2L}{\mu C_{ox} V_{eff}^2} I_{ds}$$



(a)  $W_N, W_P [\mu\text{m}/\text{mA}], V_{A_N}, V_{A_P} [\text{V}]$

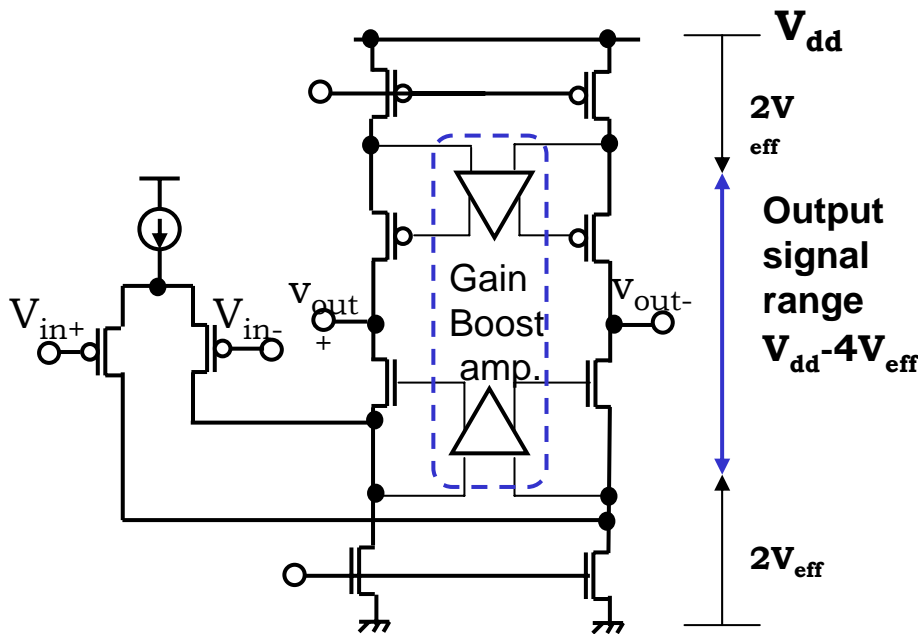
DR	$W_N$	$W_P$	$V_{A_N}$	$V_{A_P}$
90nm	24.3	74.9	0.82	0.69
0.13 $\mu\text{m}$	37.5	147	0.82	0.64
0.18 $\mu\text{m}$	54.8	219	0.99	0.93
0.25 $\mu\text{m}$	116.0	396	0.78	0.97
0.35 $\mu\text{m}$	162.0	603	1.01	0.86

(b)  $C_{pi_N}, C_{pi_P}, C_{po} [\text{fF}/\text{mA}], \omega_{p2_N}, \omega_{p2_P} [\text{GHz}]$

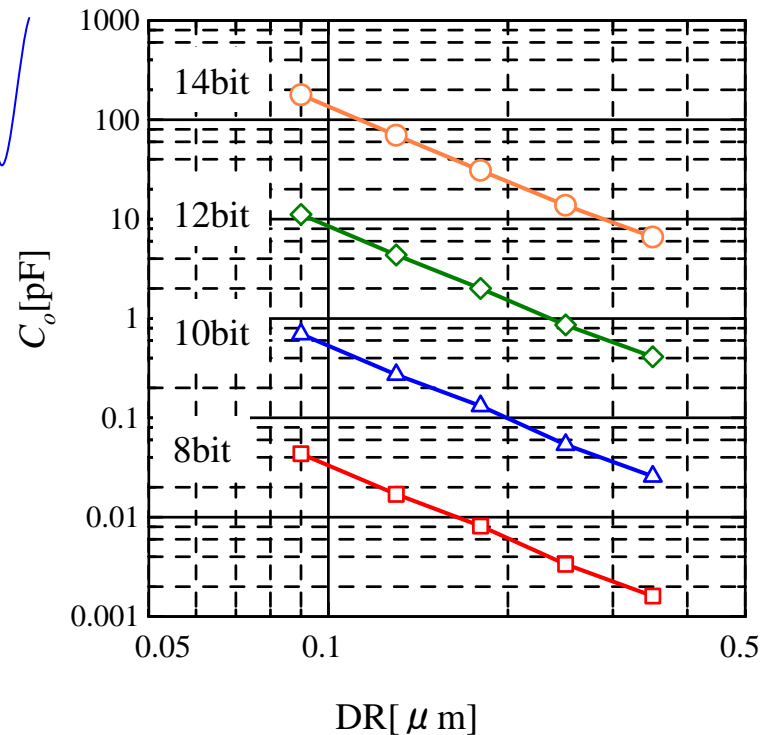
DR	$C_{pi_N}$	$C_{pi_P}$	$C_{po}$	$\omega_{p2_N}$	$\omega_{p2_P}$
90nm	23.7	93.4	94.5	9.35	15.4
0.13 $\mu\text{m}$	65.5	249	168	7.7	10.3
0.18 $\mu\text{m}$	115	475	340	2.06	4.7
0.25 $\mu\text{m}$	236	662	832	0.83	1.7
0.35 $\mu\text{m}$	303	1034	892	0.54	1.7

# Determination of signal capacitance

Larger resolution requires larger signal capacitance.  
 Furthermore, Voltage lowering increases signal capacitance more.



$$C_o \geq 1.66 \times 10^{-19} \left( \frac{2^N}{V_{sig}} \right)^2$$



	90nm	0.13 μm	0.18 μm	0.25 μm	0.35 μm
$V_{dd}$	1.2V	1.5V	1.8V	2.5V	3.3V
$V_{sig\_pp}$	1.0V	1.6V	2.2V	3.6V	5.2V

# Performance curve

Performance exhibits convex curve.

There is the peak conversion frequency and the optimum current.

Current increase results in increase of parasitic capacitances and decrease of conversion frequency in the higher current region.

$$GBW_{-close} = \frac{g_m}{2\pi C_o} \frac{1}{\left(2 + \frac{C_{pi}}{C_o}\right) \left(1 + \frac{C_{po}}{C_o}\right) + \left(1 + \frac{C_{pi}}{C_o}\right)}$$

$$g_m = \frac{2I_{ds}}{V_{eff}}, \quad C_{pi} = \alpha_i I_{ds}, \quad C_{po} = \alpha_o I_{ds}$$

$$\textcircled{1} C_o \gg C_{po}, C_{pi}$$

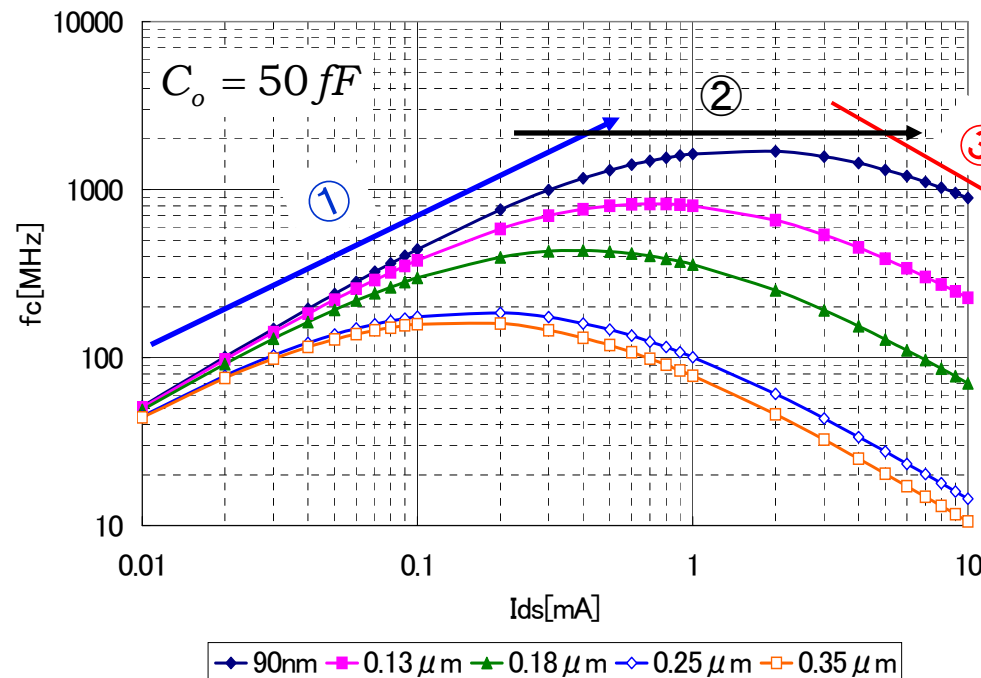
$$GBW_{-close} \approx \frac{I_{ds}}{\pi C_o V_{eff}} \cdot \frac{1}{3} \quad (\propto I_{ds})$$

$$\textcircled{2} C_{pi} < C_o < C_{po}$$

$$GBW_{-close} \approx \frac{1}{\pi C_o V_{eff}} \cdot \frac{1}{3 + \alpha_o} \quad (Constant)$$

$$\textcircled{3} C_o < C_{po}, C_o < C_{pi}$$

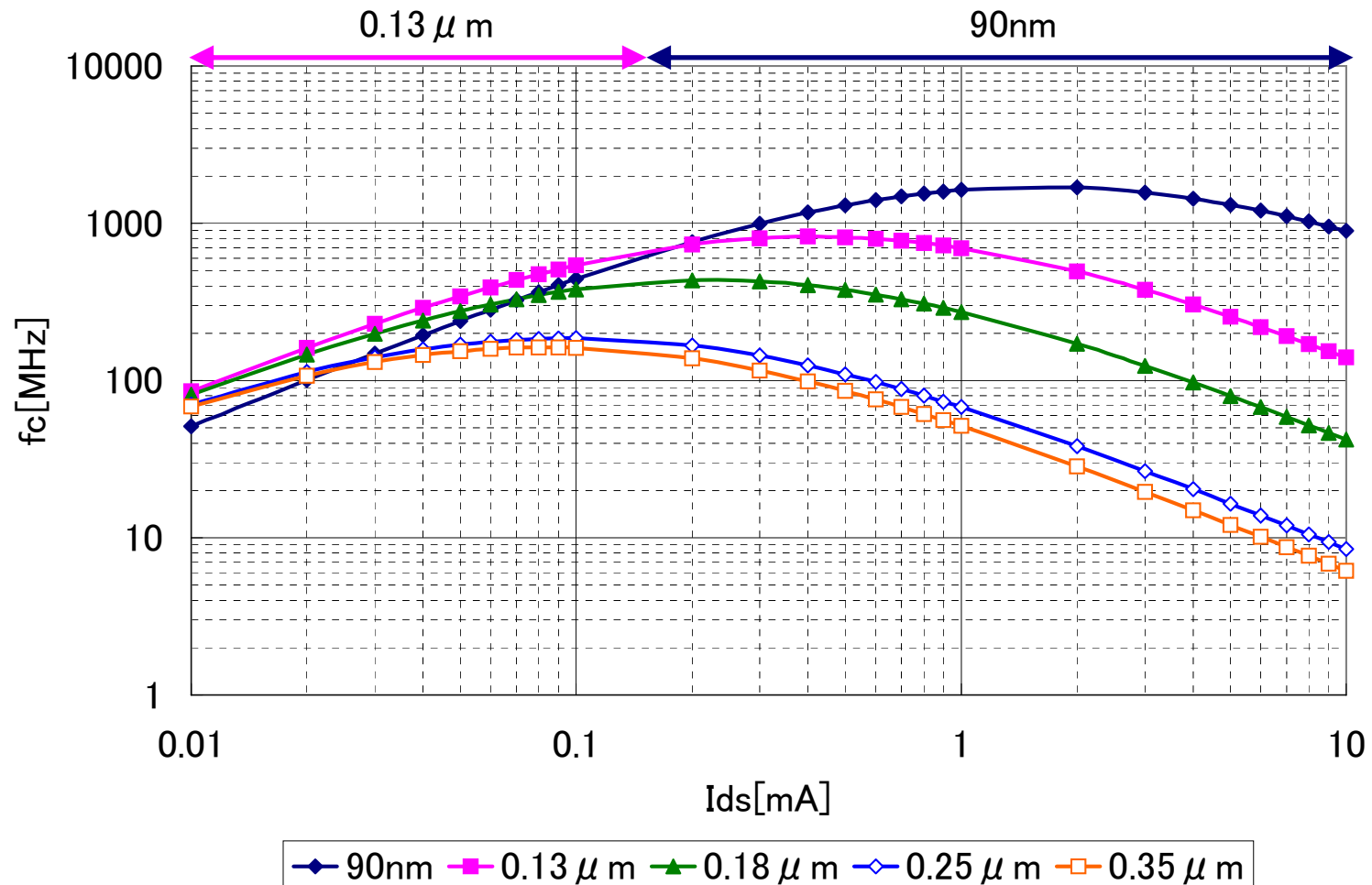
$$GBW_{-close} \approx \frac{1}{\pi C_o V_{eff}} \cdot \frac{1}{3 + \alpha_i \alpha_o I_{ds}} \quad (\propto \frac{1}{I_{ds}})$$





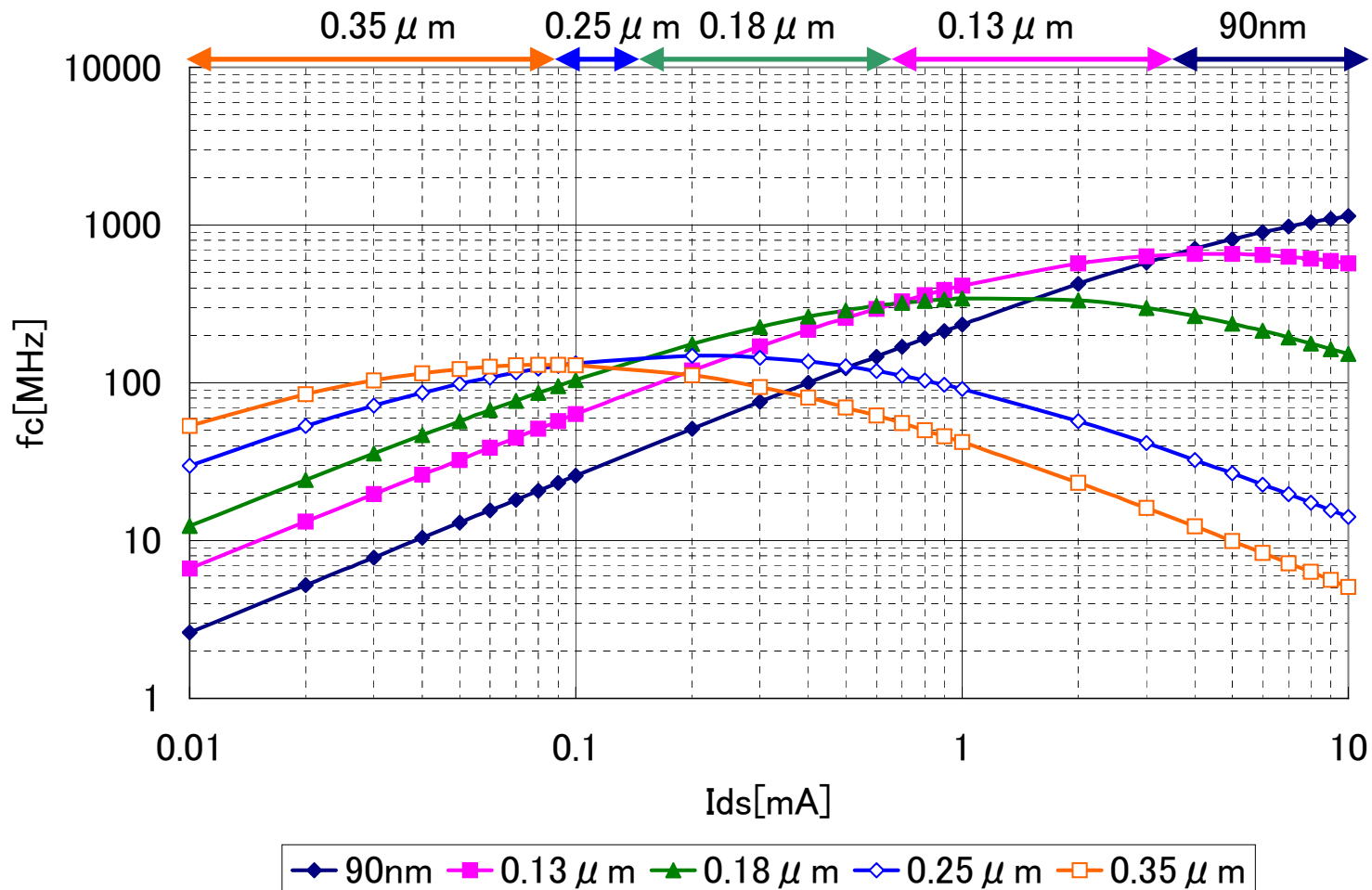
# 8 bit

0.13 $\mu\text{m}$  attains highest conversion frequency in a low current region.  
However 90nm is over striding 0.13 $\mu\text{m}$  along with increase of the current.



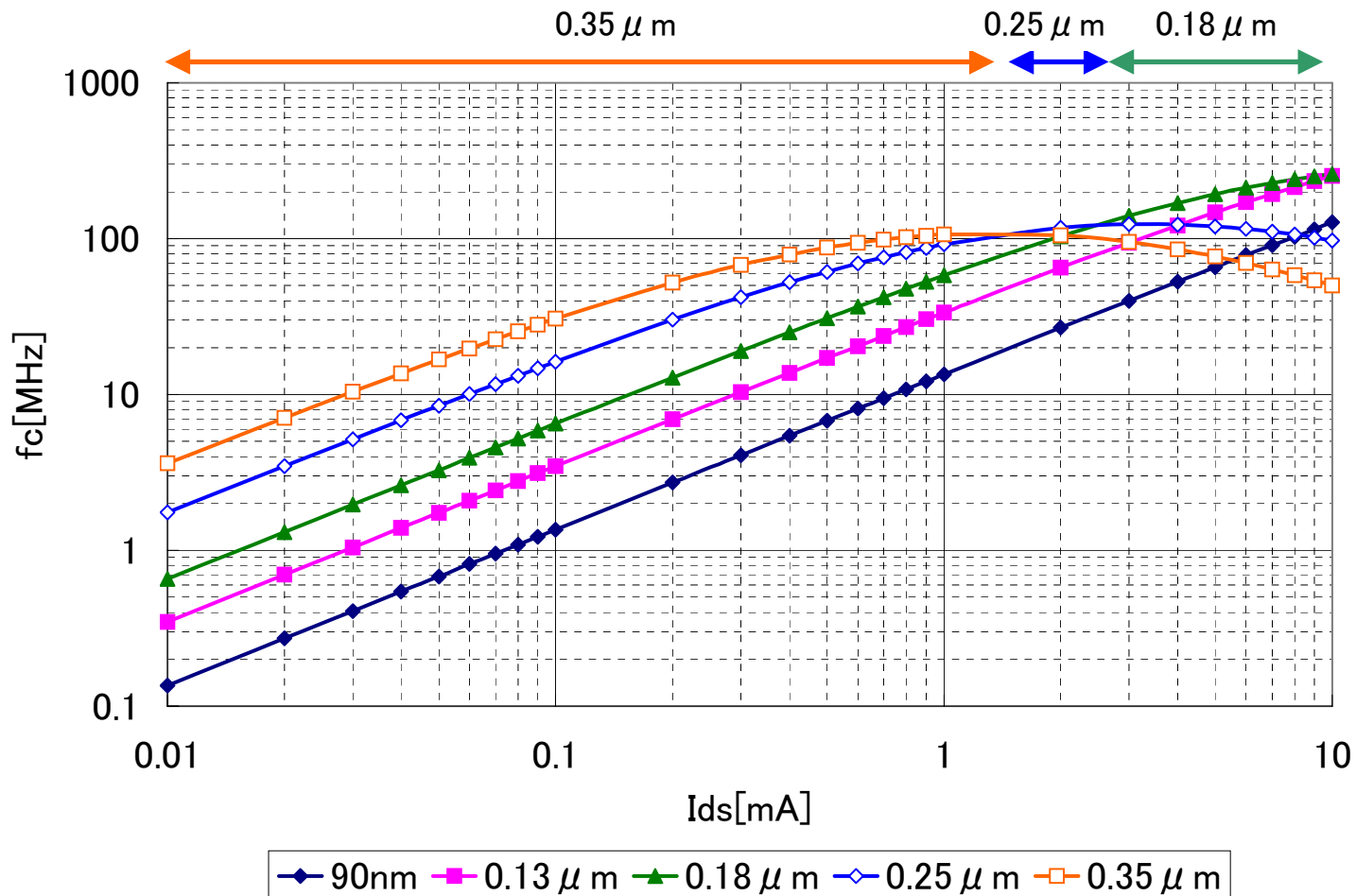
# 10 bit

The best design rule depends on operating current.  
0.35 $\mu\text{m}$  attains highest conversion frequency in low operating current region!



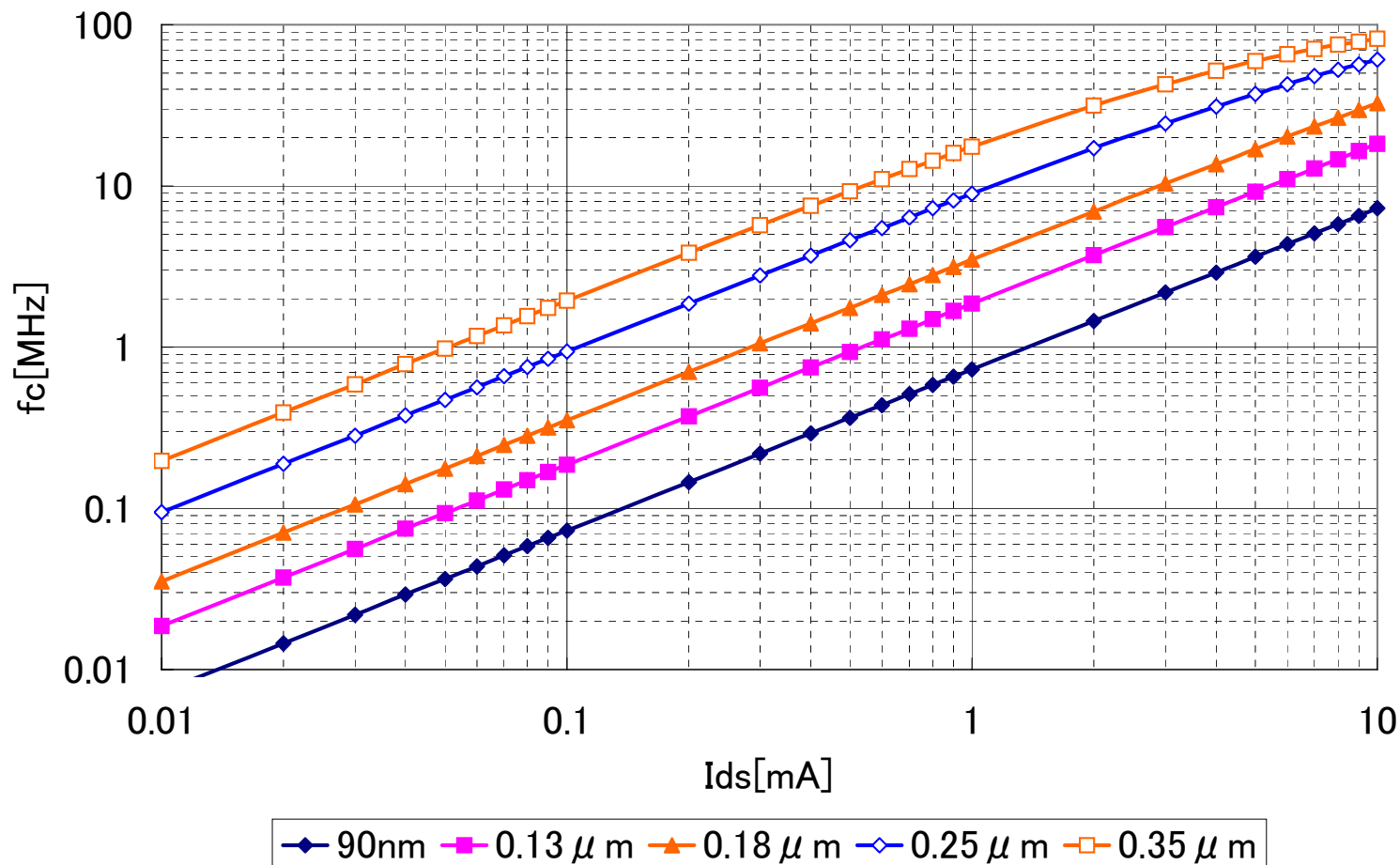
# 12 bit

Relaxed design rule is suitable for wider current range.



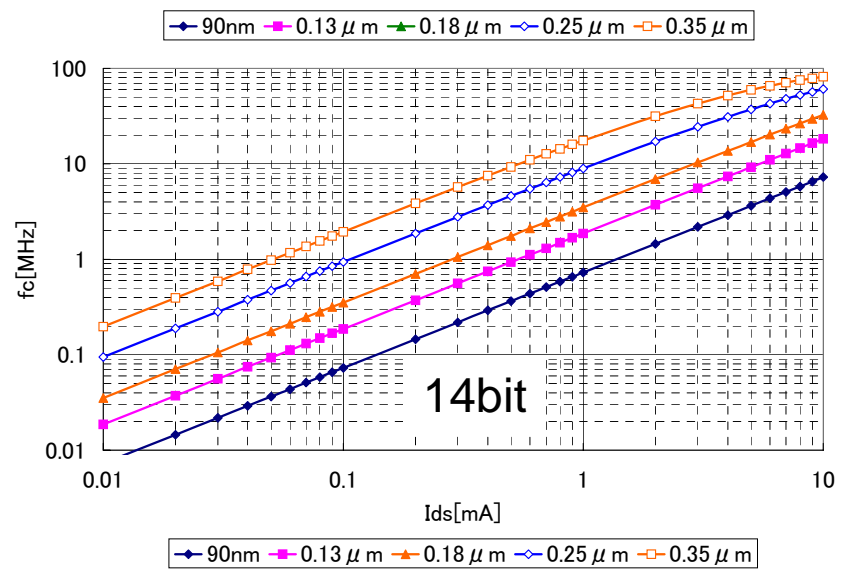
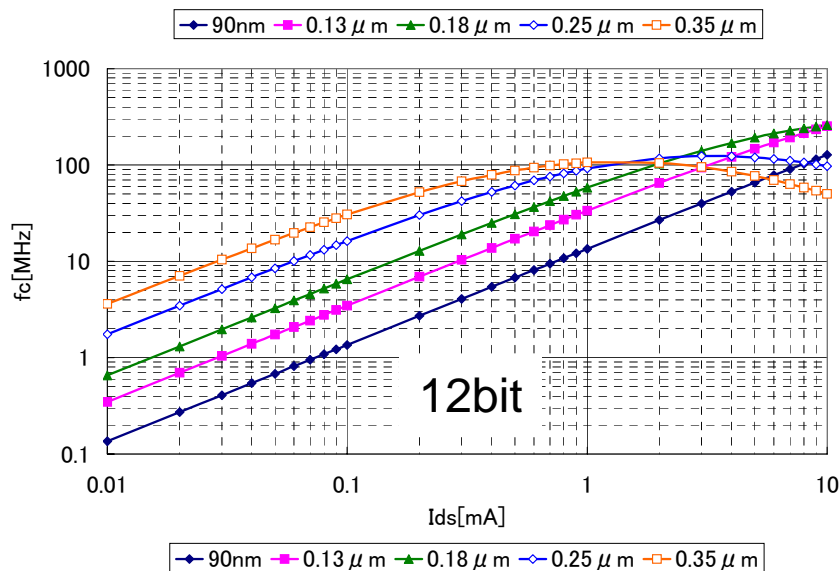
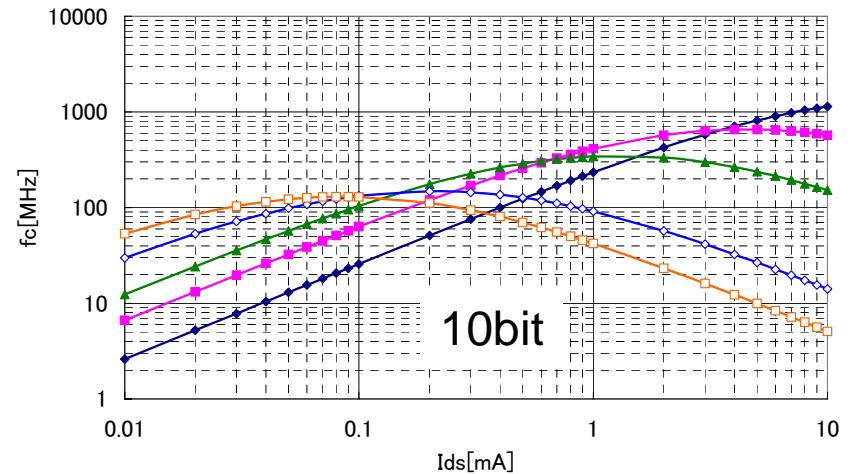
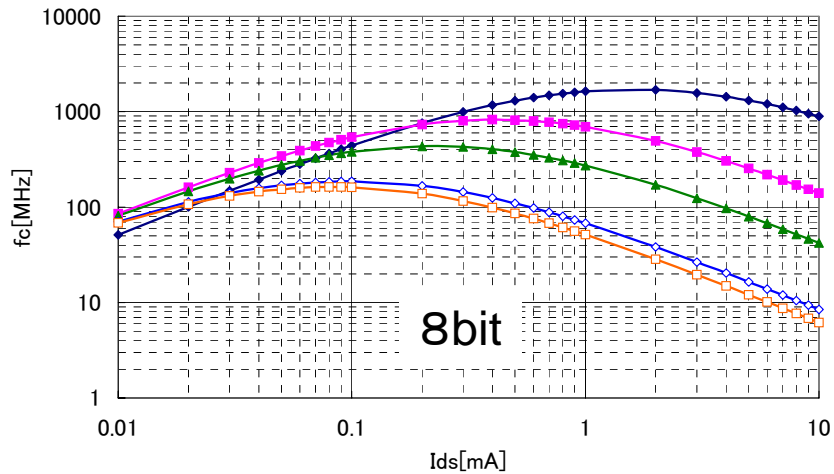
# 14 bit

Scaled CMOS is not suitable for higher resolution ADC.



# Performance summary

**Scaled CMOS is effective for just low resolution ADC.**  
**Scaled CMOS is not effective for high resolution ADC.**

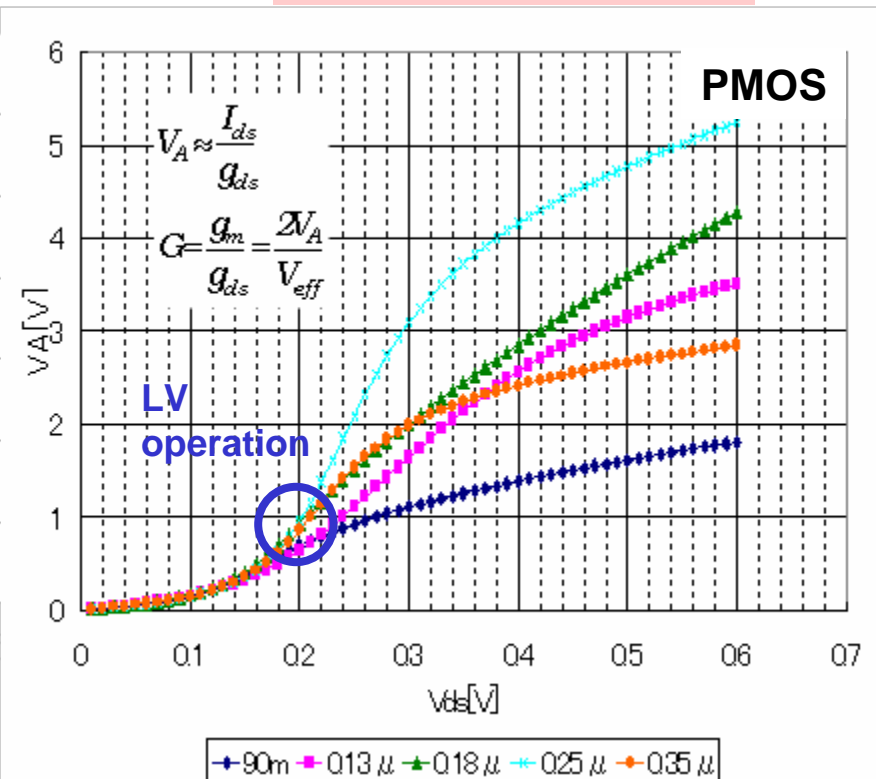
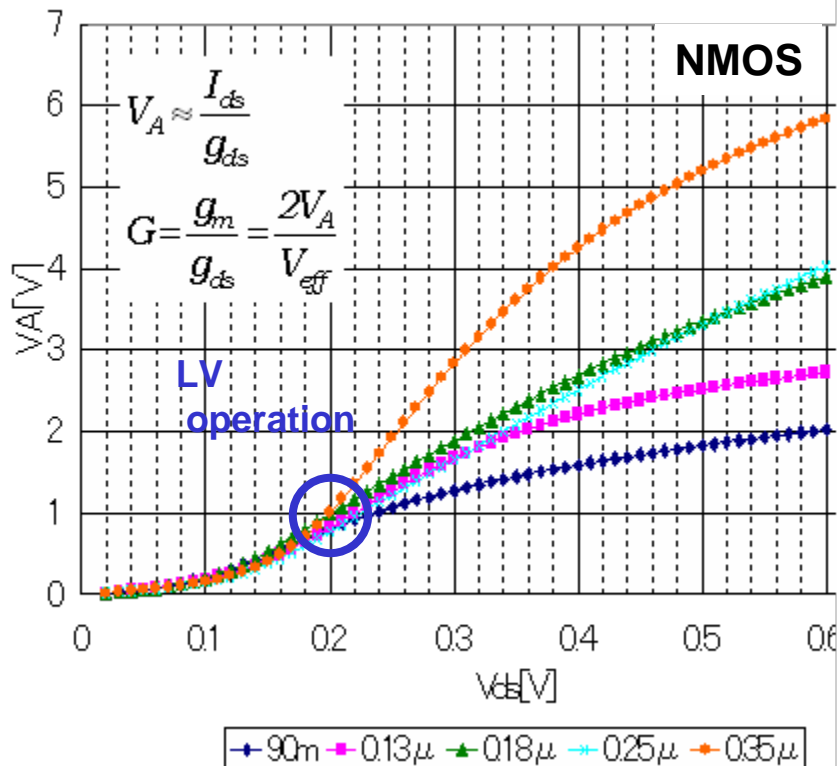


# Voltage gain

$V_A$  decreases with scaling and operating voltage lowering.  
High gain can not be expected.

$$G_i = g_m \cdot r_{ds} \quad g_m = \frac{2I_{ds}}{V_{eff}}, \quad r_{ds} = \frac{V_A}{I_{ds}}$$

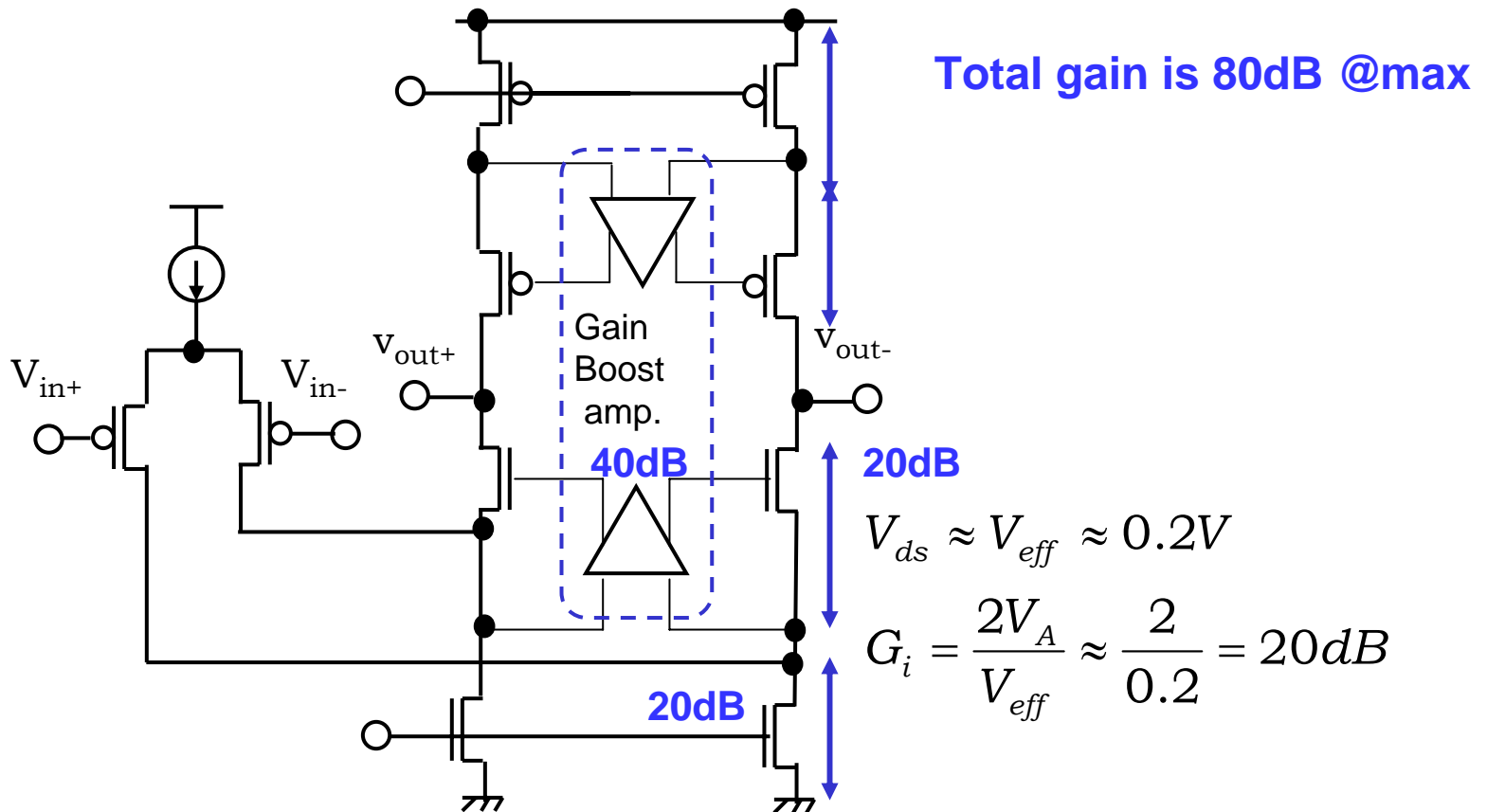
$$G_i = \frac{2V_A}{V_{eff}} \approx 10V_A$$



# Voltage gain of operational amplifier

Voltage gain of OpAmp for scaled CMOS and LV operation is 80dB at most.

Less than 10 bit ADC can be designed with scaled and low voltage CMOS.



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# **Design challenges for ADC in nano-scale era**

- No use of Operational amplifier --**
- Comparator controlled current source**
- Successive approximation ADC**
- Sub-ranging ADC**



# Design rule and Speed in Comparator

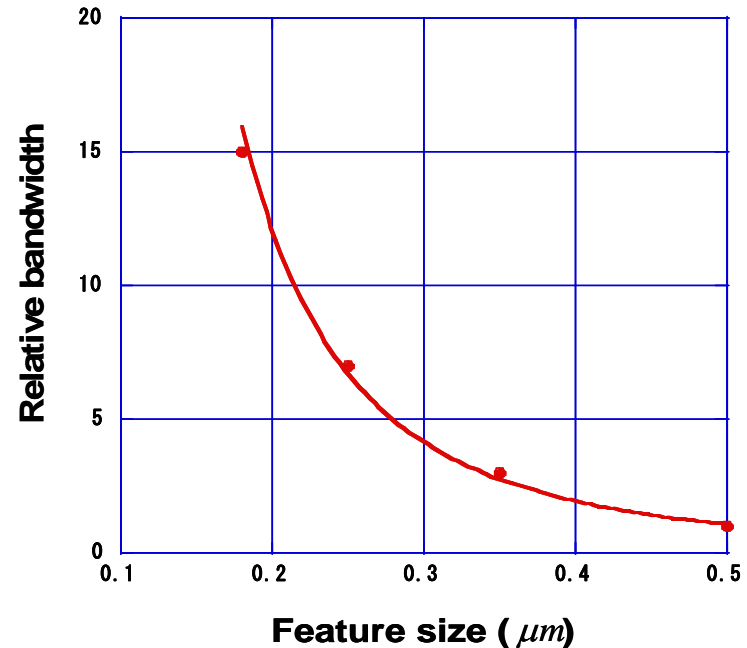
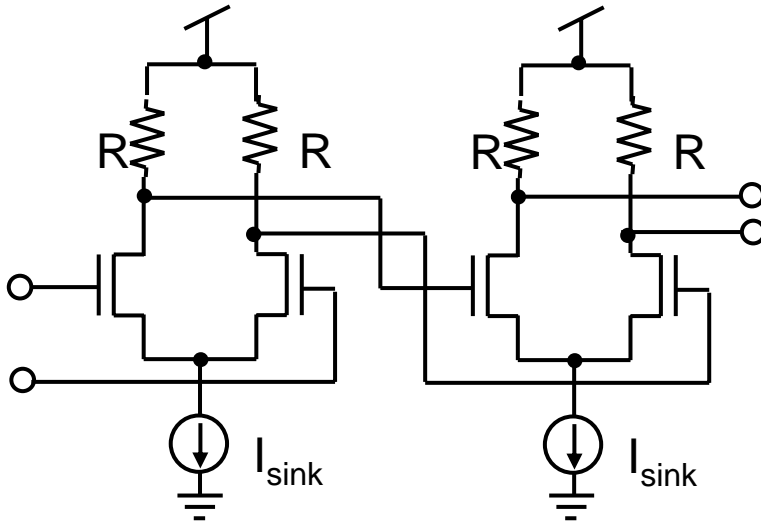
Gain bandwidth (=Speed) is inversely proportional to the  $L^2$  (channel length). Technology scaling is still effective to increase the comparator speed and to reduce operating current.

Furthermore, low voltage operation, such as 0.5V, is available.

$$GBW = \frac{g_m}{2\pi \left( WC_j + \frac{2}{3} C_{ox} LW \right)} = \frac{I_{sink}}{2\pi \left( WC_j + \frac{2}{3} C_{ox} LW \right) V_{eff}}$$

$$GBW = \frac{\mu V_{eff}}{2\pi L^2 \left( \frac{2}{3} + \frac{C_j}{k} \right)}$$

$$I_{sink} = \frac{\mu C_{ox}}{2} \frac{W}{L} V_{eff}^2 \quad C_{ox} = \frac{\kappa}{L}$$

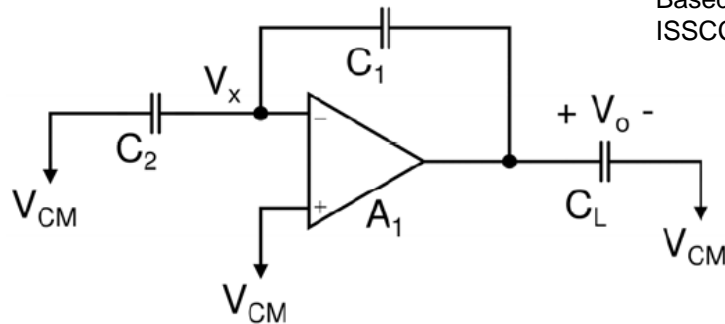


# Comparator controlled current source

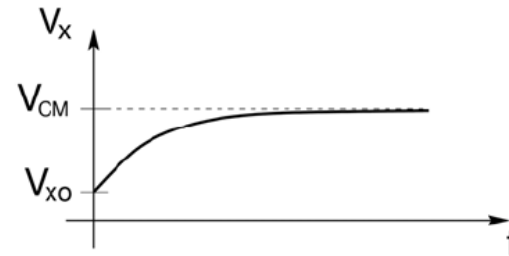
Comparator controlled current source can realize the virtual ground.

Now challenge for not use of OpAmp in ADC design has started.

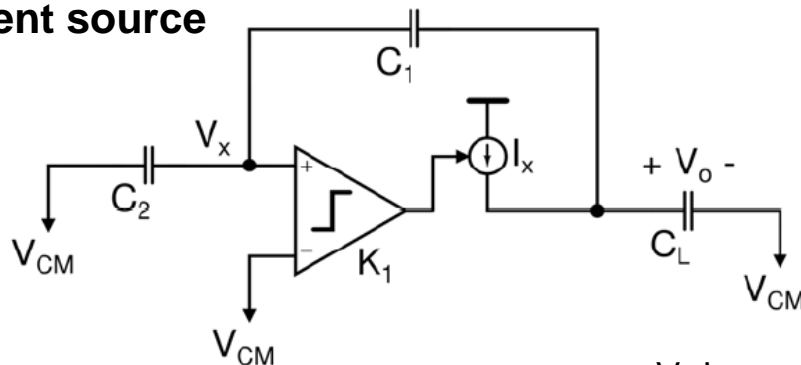
## Conventional OpAmp



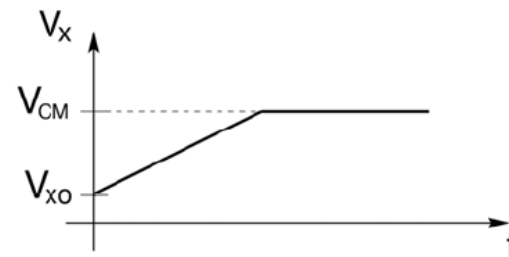
T. Sepke, J. K. Fiorenza, C. G. Sodini, P. Holloway, and H. Lee, "Comparator-Based Switched-Capacitor Circuits For Scaled CMOS Technologies," IEEE, ISSCC 2006, Dig. of Tech. Papers, pp. 574-575. Feb. 2006.



## Comparator controlled current source



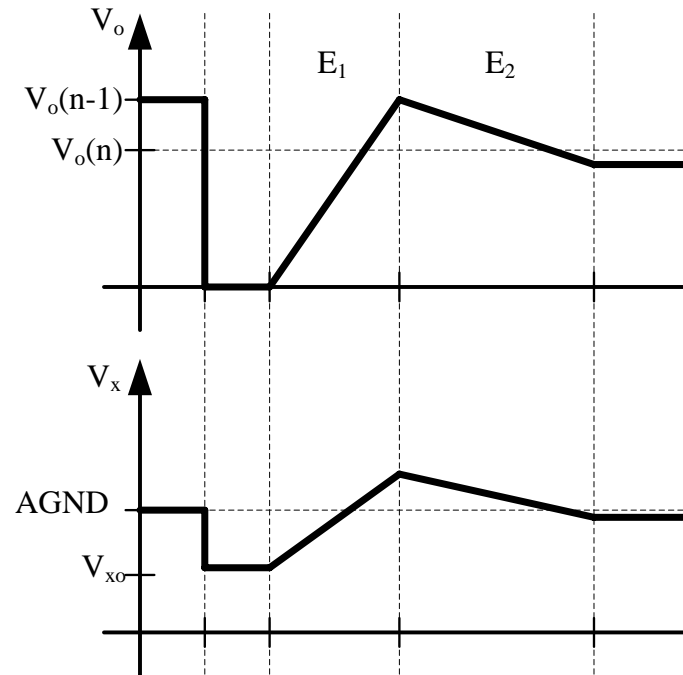
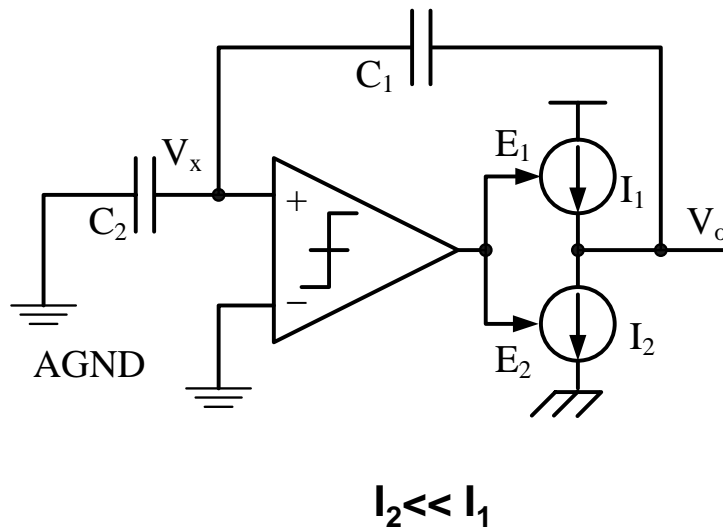
$V_x$  is reaching the virtual ground voltage asymptotically



$V_x$  is reaching the virtual ground voltage with constant rate

# Realistic comparator controlled current source

Time delay ( $V_x \rightarrow V_o$ ) causes voltage offset. Small inverse current source has been introduced. The offset voltage can be reduced and does not effect the conversion linearity.



T. Sepke, J. K. Fiorenza, C. G. Sodini, P. Holloway, and H. Lee, "Comparator-Based Switched-Capacitor Circuits For Scaled CMOS Technologies," IEEE, ISSCC 2006, Dig. of Tech. Papers, pp. 574-575. Feb. 2006.

**10b, 8MHz ADC has been developed.  
Pd=2.5mW. Lowest Pd/MHz**

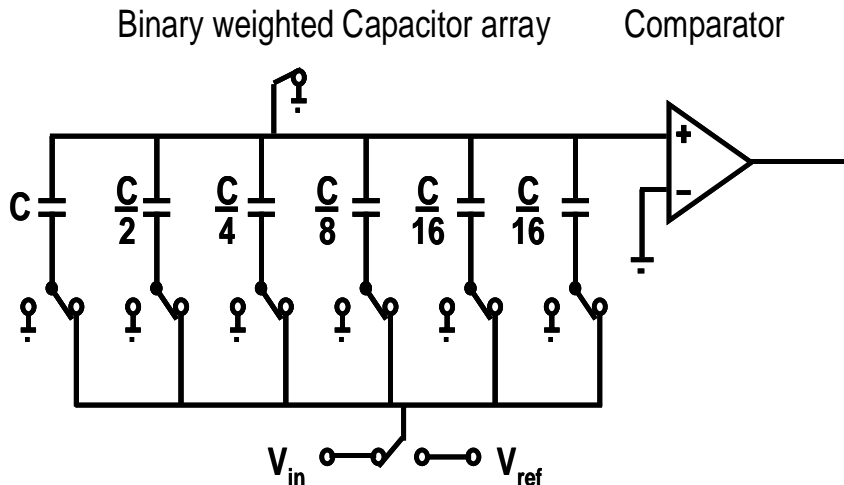
# Successive approximation ADC

Successive approximation ADC has been used long time as a low power and low speed ADC. It doesn't require OpAmp but capacitor array and comparator. Thus this architecture looks suitable for scaled and low voltage CMOS.

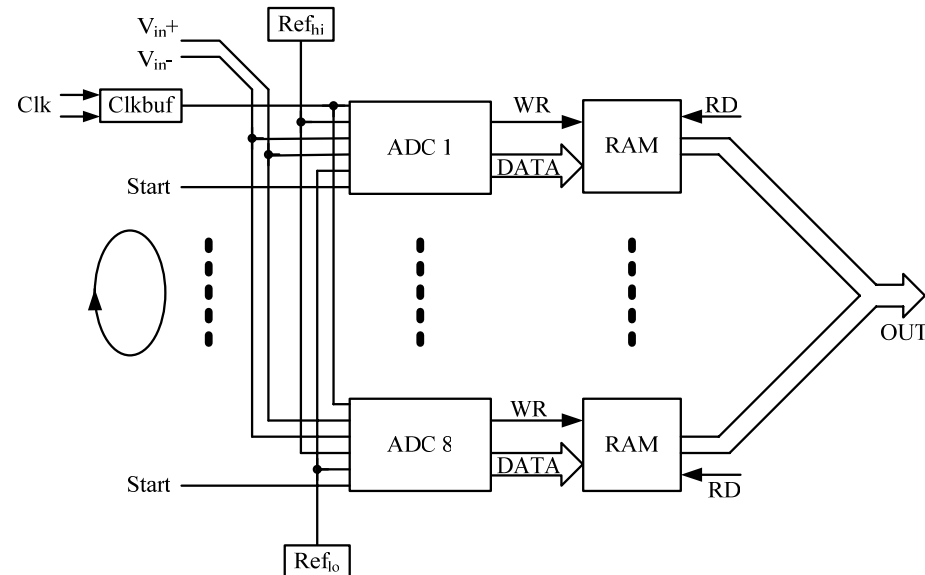
Now challenge for renewal of this conventional architecture has started.

## Successive approximation ADC

### SA-ADC



## Eight interleaved SA-ADCs with 90nm CMOS attain 600MHz operation.

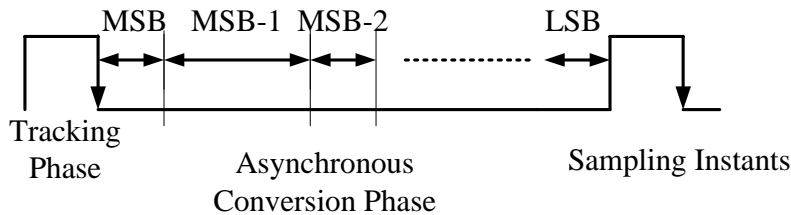
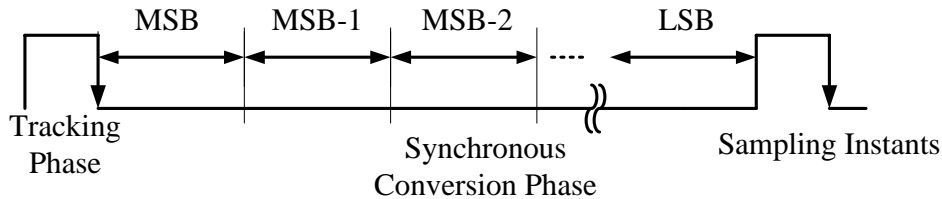


D. Draxelmayr, "A 6b 600MHz 10mW ADC Array in Digital 90nm CMOS," IEEE, ISSCC 2004, Dig. of Tech. Papers, pp. 264-265, Feb. 2004.

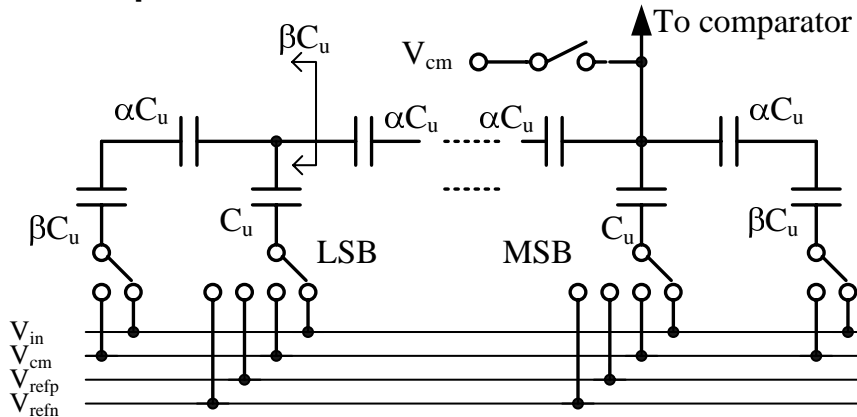
# Improvement of SA-ADC

Asynchronous clock increases conversion frequency.  
Use of proper radix reduces capacitance.

## Asynchronous clock



## Capacitor ladder with some radix number



**6bit 600MHz 5.3mW ADC has been realized with 0.13um CMOS**

$$\beta = 1 + \alpha \parallel \beta$$

$$radix = 1 + \frac{\beta}{\alpha}$$

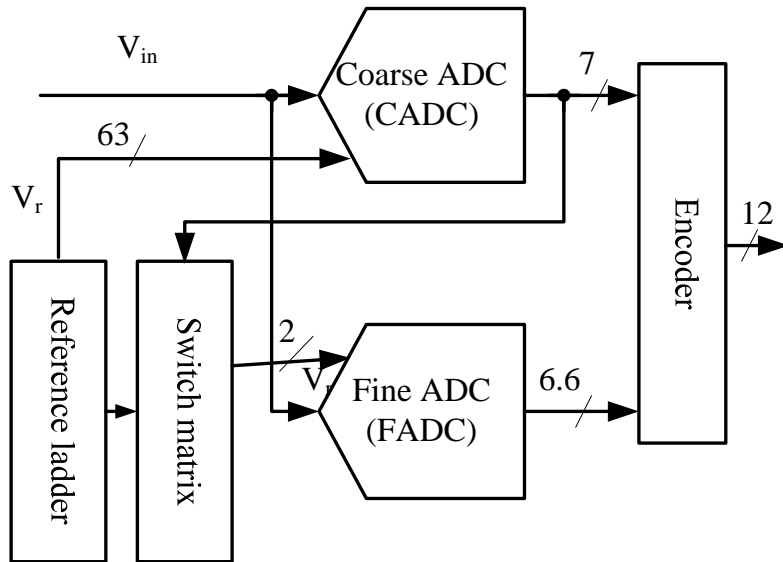
S. W. M. Chen and R. W. Brodersen, "A 6b 600MS/s 5.3mW Asynchronous ADC in 0.13um CMOS," IEEE, ISSCC 2006, Dig. of Tech. Papers, pp. 574-575. Feb. 2006.

# Sub-ranging ADC

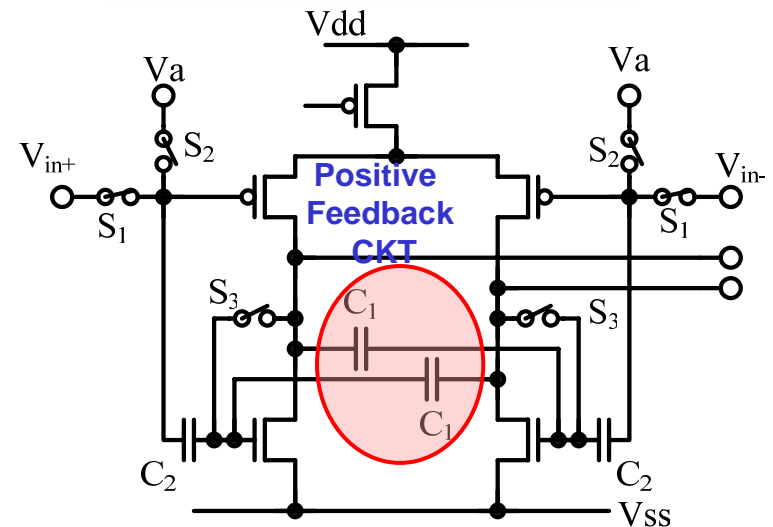
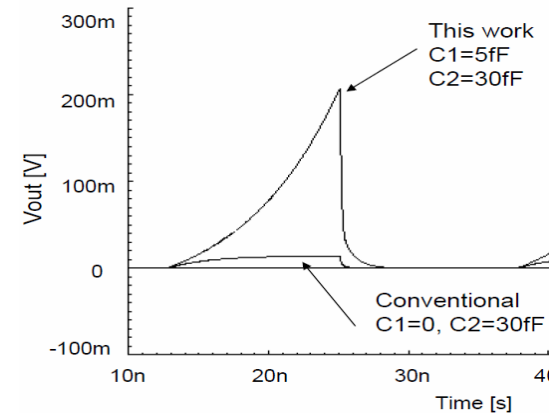
Sub-ranging ADC also doesn't require OpAmp and suitable for LV operation. However it requires low offset voltage comparators. Use of positive feedback technique has realized low offset voltage.

**Technology revival has been found.**

**Pd/MHz =0.75mW/MHz which is lowest value!!**



7]Y. Shimizu, S. Murayama, K. Kudoh, H. Yatsuda, A. Ogawa, "A 30mw 12b 40MS/s Subranging ADC with a High-Gain Offset-Canceling Positive-Feedback Amplifier in 90nm Digital CMOS," IEEE, ISSCC 2006, Dig. of Tech. Papers, pp. 222-225. Feb. 2006.



# Summary

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- **Technology scaling is effective for increasing analog performance if not so much higher SNR is required.**
- **Technology scaling is not effective for increasing analog performance if higher SNR is required, and sometimes degrades it.**
- **Increase of signal capacitance to keep the SNR high at low voltage operation is essential serious issue for use of scaled CMOS.**
- **Furthermore, Gain lowering of OpAmp due to technology scaling and voltage lowering becomes serious issues.**
- **Design challenges for ADC has been started.**
- **No use of OpAmp is a common idea.**
- **Technology revivals have been found and the performance has been improved. Further improvement will be expected in future.**